On the Grunwald problem for regular Galois groups over $\mathbb Q$

François LEGRAND
Technion - Israel Institute of Technology

Let G be a finite group. Given a finite set S of prime numbers and, for each $p \in S$, a Galois extension F_p/\mathbb{Q}_p with Galois group embedding into G, the Grunwald problem asks whether there exists a Galois extension of \mathbb{Q} with Galois group G which approximates the local extensions F_p/\mathbb{Q}_p $(p \in S)$. We investigate to what extent the set of specializations of a given regular Galois extension of $\mathbb{Q}(T)$ with Galois group G can provide answers to this question.